

**5.208 max\_nvalue**

	DESCRIPTION	LINKS	GRAPH	AUTOMATON
<b>Origin</b>	Derived from <a href="#">nvalue</a> .			
<b>Constraint</b>	<code>max_nvalue(MAX, VARIABLES)</code>			
<b>Arguments</b>	MAX : <a href="#">dvar</a> VARIABLES : <a href="#">collection</a> ( <code>var-dvar</code> )			
<b>Restrictions</b>	$MAX \geq 1$ $MAX \leq  VARIABLES $ <a href="#">required</a> (VARIABLES, var)			
<b>Purpose</b>	MAX is the maximum number of times that the same value is taken by the variables of the collection VARIABLES.			
<b>Example</b>	<div style="border: 1px solid blue; padding: 10px; display: inline-block;"> <math display="block">3, \left( \begin{array}{c} \text{var} - 9, \\ \text{var} - 1, \\ \text{var} - 7, \\ \text{var} - 1, \\ \text{var} - 1, \\ \text{var} - 6, \\ \text{var} - 7, \\ \text{var} - 7, \\ \text{var} - 4, \\ \text{var} - 9 \end{array} \right)</math> </div>			
	In the example, values 1, 4, 6, 7, 9 are respectively used 3, 1, 1, 3, 2 times. So the maximum number of time MAX that a same value occurs is 3. Consequently the <code>max_nvalue</code> constraint holds.			
<b>Symmetries</b>	<ul style="list-style-type: none"> <li>Items of VARIABLES are <a href="#">permutable</a>.</li> <li>All occurrences of two distinct values of VARIABLES.var can be <a href="#">swapped</a>; all occurrences of a value of VARIABLES.var can be <a href="#">renamed</a> to any unused value.</li> </ul>			
<b>Usage</b>	This constraint may be used in order to replace a set of <a href="#">count</a> or <a href="#">among</a> constraints were one would have to generate explicitly one constraint for each potential value. Also useful for constraining the number of occurrences of the mostly used value without knowing this value in advance and without giving explicitly an upper limit on the number of occurrences of each value as it is done in the <a href="#">global_cardinality</a> constraint.			
<b>Reformulation</b>	Assume that VARIABLES is not empty. Let $\alpha$ and $\beta$ respectively denote the smallest and largest possible values that can be assigned to the variables of the VARIABLES collection. Let the variables $O_\alpha, O_{\alpha+1}, \dots, O_\beta$ respectively correspond to the number of occurrences of values $\alpha, \alpha + 1, \dots, \beta$ within the variables of the VARIABLES collection.			

The `max_nvalue` constraint can be expressed as the conjunction of the following two constraints:

```

global_cardinality (VARIABLES,
                   ⟨val - α noccurrence - Oα,
                     val - α + 1 noccurrence - Oα+1,
                     ...
                     val - β noccurrence - Oβ⟩),
maximum (MAX, ⟨Oα, Oα+1, ..., Oβ⟩).

```

**See also**

**common keyword:** `among` (*counting constraint*), `count`,  
`global_cardinality` (*value constraint*, *counting constraint*), `min_nvalue`,  
`nvalue` (*counting constraint*).

**Keywords**

**application area:** assignment.

**characteristic of a constraint:** maximum, automaton, automaton with array of counters.

**constraint type:** value constraint, counting constraint.

**final graph structure:** equivalence.

**modelling:** maximum number of occurrences.

<b>Arc input(s)</b>	VARIABLES
<b>Arc generator</b>	<i>CLIQUE</i> $\mapsto$ <code>collection(variables1, variables2)</code>
<b>Arc arity</b>	2
<b>Arc constraint(s)</b>	<code>variables1.var = variables2.var</code>
<b>Graph property(ies)</b>	<u><i>MAX_NSCC</i></u> = MAX

**Graph model**

Because of the arc constraint, each strongly connected component of the final graph corresponds to a distinct value that is assigned to a subset of variables of the `VARIABLES` collection. Therefore the number of vertices of the largest strongly connected component is equal to the mostly used value.

Parts (A) and (B) of Figure 5.402 respectively show the initial and final graph associated with the **Example** slot. Since we use the `MAX_NSCC` graph property, we show the largest strongly connected component of the final graph.

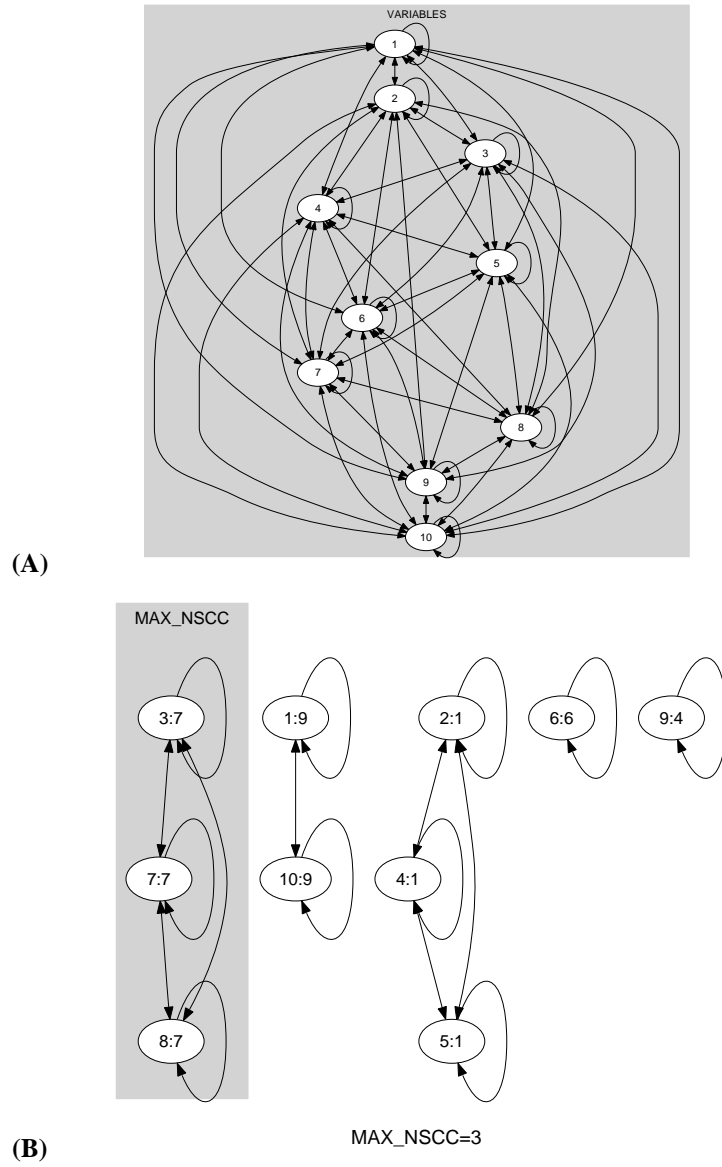


Figure 5.402: Initial and final graph of the max\_nvalue constraint

**Automaton**

Figure 5.403 depicts the automaton associated with the `max_nvalue` constraint. To each item of the collection `VARIABLES` corresponds a signature variable  $S_i$  that is equal to 0.

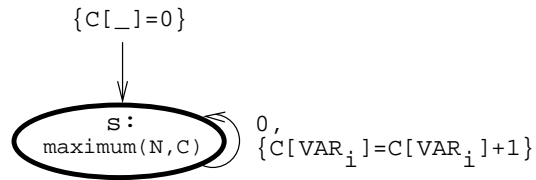


Figure 5.403: Automaton of the `max_nvalue` constraint

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