

5.122 element_sparse

	DESCRIPTION	LINKS	GRAPH	AUTOMATON
Origin	CHIP			
Constraint	<code>element_sparse</code> (ITEM, TABLE, DEFAULT)			
Usual name	element			
Arguments	ITEM : <code>collection</code> (index-dvar, value-dvar) TABLE : <code>collection</code> (index-int, value-int) DEFAULT : <code>int</code>			
Restrictions	<code>required</code> (ITEM, [index, value]) ITEM.index ≥ 1 ITEM = 1 <code>required</code> (TABLE, [index, value]) TABLE.index ≥ 1 <code>distinct</code> (TABLE, index)			
Purpose	<div style="border: 1px solid pink; padding: 5px;"> ITEM[1].value is equal to one of the entries of the table TABLE or to the default value DEFAULT if the entry ITEM[1].index does not exist in TABLE. </div>			
Example	$\left(\left\langle \begin{array}{l} \langle \text{index} - 2 \text{ value} - 5 \rangle, \\ \text{index} - 1 \quad \text{value} - 6, \\ \langle \text{index} - 2 \quad \text{value} - 5, \\ \text{index} - 4 \quad \text{value} - 2, \\ \text{index} - 8 \quad \text{value} - 9 \end{array} \right\rangle, 5 \right)$			
	The <code>element_sparse</code> constraint holds since its first argument ITEM corresponds to the second item of the TABLE collection.			
Typical	TABLE > 1 <code>range</code> (TABLE.value) > 1			
Symmetries	<ul style="list-style-type: none"> • Items of TABLE are <code>permutable</code>. • All occurrences of two distinct values in ITEM.value, TABLE.value or DEFAULT can be <code>swapped</code>; all occurrences of a value in ITEM.value, TABLE.value or DEFAULT can be <code>renamed</code> to any unused value. 			
Usage	A sometimes more compact form of the <code>element</code> constraint: we are not obliged to specify explicitly the table entries that correspond to the specified default value. This can sometimes reduce drastically memory utilisation.			
Remark	The original constraint of CHIP had an additional parameter SIZE giving the maximum value of ITEM.index.			

Reformulation

Let I and V respectively denote $ITEM[1].index$ and $ITEM[1].value$. The `element_sparse`($ITEM, TABLE, DEFAULT$) constraint can be expressed in term of a reified constraint of the form:

$$\begin{aligned} & ((I = TABLE[1].index \wedge V = TABLE[1].value) \vee \\ & (I = TABLE[2].index \wedge V = TABLE[2].value) \vee \\ & \dots \\ & (I = TABLE[|TABLE|].index \wedge V = TABLE[|TABLE|].value)) \vee \\ & ((I \neq TABLE[1].index) \wedge \\ & (I \neq TABLE[2].index) \wedge \\ & \dots \\ & (I \neq TABLE[|TABLE|].index) \wedge \\ & (V = DEFAULT)). \end{aligned}$$
See also

common keyword: `elem`, `element` (*array constraint*), `elements_sparse` (*sparse table*).

implies: `elements_sparse`.

system of constraints: `elements_sparse`.

Keywords

characteristic of a constraint: `automaton`, `automaton without counters`, `reified automaton constraint`, `derived collection`.

constraint arguments: `binary constraint`.

constraint network structure: `centered cyclic(2) constraint network(1)`.

constraint type: `data constraint`.

filtering: `arc-consistency`.

modelling: `array constraint`, `table`, `sparse table`, `sparse functional dependency`, `variable indexing`.

Derived Collections

$$\text{col} \left(\begin{array}{l} \text{DEF-collection}(\text{index-int}, \text{value-int}), \\ [\text{item}(\text{index} - 0, \text{value} - \text{DEFAULT})] \end{array} \right)$$

$$\text{col} \left(\begin{array}{l} \text{TABLE_DEF-collection}(\text{index-dvar}, \text{value-dvar}), \\ [\text{item}(\text{index} - \text{TABLE.index}, \text{value} - \text{TABLE.value}), \\ \text{item}(\text{index} - \text{DEF.index}, \text{value} - \text{DEF.value})] \end{array} \right)$$
Arc input(s)

ITEM TABLE_DEF

Arc generator*PRODUCT* \mapsto *collection*(item, table_def)**Arc arity**

2

Arc constraint(s)

- item.value = table_def.value
- item.index = table_def.index \vee table_def.index = 0

Graph property(ies) $\overline{\text{NARC}} \geq 1$ **Graph model**

The final graph has between one and two arc constraints: it has two arcs when the default value DEFAULT occurs also in the table TABLE; otherwise it has only one arc.

Parts (A) and (B) of Figure 5.250 respectively show the initial and final graph associated with the **Example** slot. Since we use the $\overline{\text{NARC}}$ graph property the arcs of the final graph are outline with thick lines.

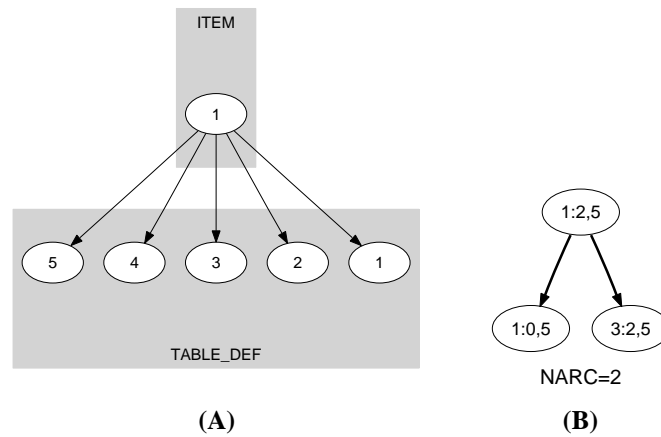


Figure 5.250: Initial and final graph of the *element_sparse* constraint

Automaton

Figure 5.251 depicts the automaton associated with the `element_sparse` constraint. Let `INDEX` and `VALUE` respectively be the index and the value attributes of the unique item of the `ITEM` collection. Let `INDEXi` and `VALUEi` respectively be the index and the value attributes of the *i*th item of the `TABLE` collection. To each quintuple $(INDEX, VALUE, DEFAULT, INDEX_i, VALUE_i)$ corresponds a signature variable S_i as well as the following signature constraint:

$$\left\{ \begin{array}{l} (INDEX \neq INDEX_i \wedge VALUE \neq DEFAULT) \Leftrightarrow S_i = 0 \wedge \\ (INDEX = INDEX_i \wedge VALUE = VALUE_i) \Leftrightarrow S_i = 1 \wedge . \\ (INDEX \neq INDEX_i \wedge VALUE = DEFAULT) \Leftrightarrow S_i = 2 \end{array} \right.$$

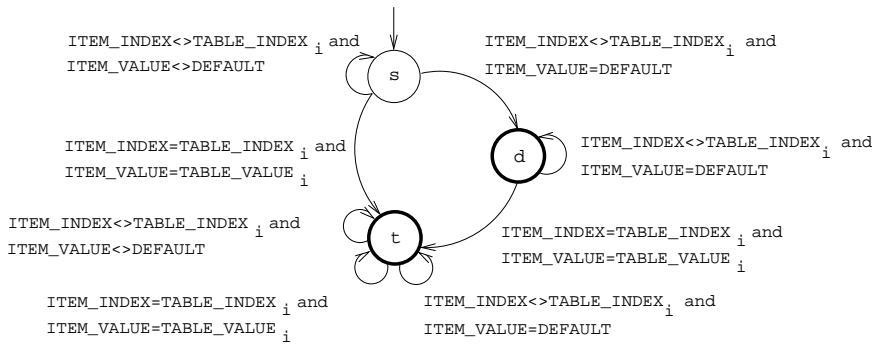


Figure 5.251: Automaton of the `element_sparse` constraint

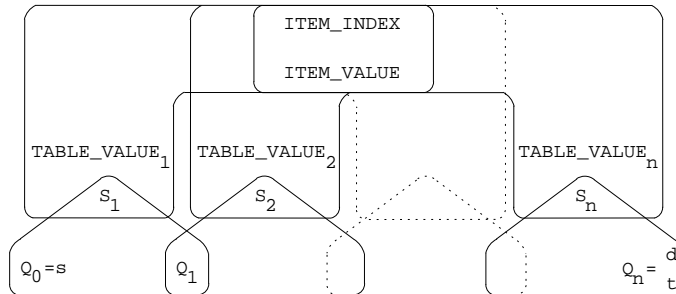


Figure 5.252: Hypergraph of the reformulation corresponding to the automaton of the `element_sparse` constraint